## Algebra 2H

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## Sections 8.1 and 8.2 Homework Day 1

Marge accepted a job where she will make $\$ 35,000$. Each year, she will get a $4 \%$ pay increase. Complete the chart below to determine how much she will earn after tyears.

| \# years, $\mathbf{t}$ | $4 \%$ increase | New Salary |
| :--- | :--- | :--- |
| 0 | - | 30,000 |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 5 |  |  |

## Exponential Growth and Exponential Decay Models

When a quantity increases by a fixed percent each time period, it can be modeled by an exponential growth function:

$$
y=a(1+r)^{t}
$$

When a quantity decreases by a fixed percent each time period, it can be modeled by an exponential decay function:

$$
y=a(1-r)^{t}
$$

$y$ is the amount after $t$ time periods, $a$ is the initial amount and $r$ is the percent growth/decay expressed as a decimal.
$(1+r)$ is the growth factor
$(1-r)$ is the decay factor

## Problems:

1. For the problem above (Marge), determine whether the situation represents exponential growth or exponential decay.
a) Write an equation to model the situation:
b) How much will she earn after 10 years? $\qquad$
c) How many years would it take until she earns more than $\$ 80,000$ years annually? $\qquad$
2. A car depreciates at a rate of $21 \%$ a year. The car originally costs $\$ 26,000$.

Does this represent exponential growth or decay? $\qquad$
a) Write an equation to model the situation:
b) How much will the car be worth after 8 years? $\qquad$
c) When will the car be worth less than half of its original value?
3. The amount (in milligrams) of a drug in the body $t$ hours after taking a pill is given by : $A(t)=200(0.75)^{t}$
a) What is the initial dosage given? $\qquad$
b) What percent of the drug leaves the body each hour? $\qquad$
c) How many milligrams of the drug will be left in the body after 8 hours? $\qquad$
d) How many hours will it take until there are less than 5 mg of the drug in the body? $\qquad$
4. A rapidly decaying radioactive material's half-life is every 9 hours. The material originally has 500 mg of radioactive material.
a) Write a model to represent this situation (what time period does $t$ represent?)
b) How much radioactive material will be left after 45 hours? $\qquad$
c) How much radioactive material will be left after 8 days?

Compound Interest - is interest paid on an initial investment, called the principal, and on previously earned interest.

If an initial investment, $P$, is in an account that pays an annual rate, $r$ (as a decimal), compounded $n$ times per year, then the amount, $A$, in the account after $t$ years is:

$$
A=P\left(1+\frac{r}{n}\right)^{n t}
$$

## Examples:

1. You deposit $\$ 100,000$ in an account that earns $2.5 \%$ annual interest. Find the balance after three years if the interest is compounded:
a) annually
b) quarterly
c) monthly
d) daily
2. You want to have $\$ 10,000$ in your account after 5 years. Find the amount your initial deposit should be for each situation:
a) The account pays $3.5 \%$ annual interest compounded monthly.
b) The account pays $4.25 \%$ annual interest compounded yearly.
